

MATH Problem 3.

Let α be an angle of the triangle. Prove that the radius of its circumscribed circle can be R , and the radius of its inscribed circle can be r if and only if

$$\sin \frac{\alpha}{2} \left(1 - \sin \frac{\alpha}{2} \right) \geq \frac{r}{2R}.$$